

How much does winning ACM depend on practice?

We assume that  $p$ , the probability that a given team will win a given contest, is related to  $n$ , the number of practice problems solved by the team prior to the contest. This relationship is modelled by the *logistic* formula

$$\log(p/(1-p)) = a + bn,$$

for some  $a$  and  $b$ . Your job is to find  $a$  and  $b$  such that the formula most accurately reflects a set of observed results.

Each observation consists of  $n$  and  $w$ .  $n$  is the number of practice problems solved by some team prior to a contest, and  $w$  is 1 if the team wins the contest, 0 if it does not.

Given  $a$ ,  $b$ , and  $n$  the formula above may be used to compute  $p$ , the estimated probability that  $w = 1$ . The *likelihood* of a particular observation is  $p$  if  $w = 1$  and  $1 - p$  if  $w = 0$ ; The likelihood of a set of observations is the product of the likelihoods of the individual observations.

You are to compute the *maximum likelihood estimate* for  $a$  and  $b$ . That is, the values of  $a$  and  $b$  for which the likelihood of a given set of observations is maximized.



## Input

The input contains several test cases followed by a line containing 0. Each test case begins with  $1 < k \leq 100$ , the number of observations that follow. Each observation consists of integers  $0 \leq n \leq 100$  and  $0 \leq w \leq 1$ . The input will contain at least two distinct values of  $n$  and of  $w$ .

## Output

For each test case, output a single line containing  $a$  and  $b$ , rounded to four digits to the right of the decimal.

## Sample Input

```
20
0 0
0 0
0 0
0 0
0 0
1 0
1 0
1 0
1 1
2 0
2 0
2 1
2 1
3 0
3 1
3 1
3 1
4 1
4 1
4 1
4 1
0
```

## Sample Output

```
-3.1748 1.5874
```